

## Module - IV

Database Design: Functional Dependencies - Normal forms; First Normal form, Second Normal Form, Third Normal Form, Boyce Codd Normal Form, Multivalued Dependencies & Fourth Normal Form, Join Dependencies & Fifth Normal form. Inference Rules for Functional Dependencies. Minimal sets of functional Dependencies, Prop: of Rdnl decomposition.



# Functional Dependency

A f.d is a constraint b/w two sets of attributes from the db, denoted by,

$$X \rightarrow Y$$

Y is functionally dependent on X.

## ⊗ Inference Rules for Functional Dependency

- (1) Reflexive Rule :- If  $Y \subseteq X$ , then  $X \rightarrow Y$
- (2) Augmentation Rule :- If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$
- (3) Transitive Rule :- If  $X \rightarrow Y$  &  $Y \rightarrow Z$ , then  $X \rightarrow Z$ .
- (4) Decomposition or Projective Rule : If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  &  $X \rightarrow Z$ .
- (5) Union or Additive Rule : If  $X \rightarrow Y$  &  $X \rightarrow Z$ , then  $X \rightarrow YZ$
- (6) Pseudo Transitive Rule :- If  $X \rightarrow Y$  &  $WY \rightarrow Z$ , then  $WX \rightarrow Z$ .

The 1st 3 rules are

- sound :- generate only f.d that actually hold.
- complete :- generate all f.d that hold. They are called Armstrong's axioms, the last 3 inference rules are inferred from armstrong's axioms.

### Examples

$$R = (A, B, C, G, H, I)$$

$$F = \left\{ \begin{array}{l} A \rightarrow B \\ A \rightarrow C \end{array} \right\}$$

$$CG \rightarrow H$$

$$CG \rightarrow I$$

$$B \rightarrow H$$

find f.d  $F^+$  of  $F$ .



By transitivity from  $A \rightarrow B$  &  $B \rightarrow H$   
we get  $A \rightarrow H$ .

(2)  $AH \rightarrow I$

by augmentation  $A \rightarrow C$  with  $H$ , to get  $AH \rightarrow CH$   
& then transitivity with  $CH \rightarrow I$

(3)  $CH \rightarrow HI$

from  $CH \rightarrow H$  &  $CH \rightarrow I$  (union rule).

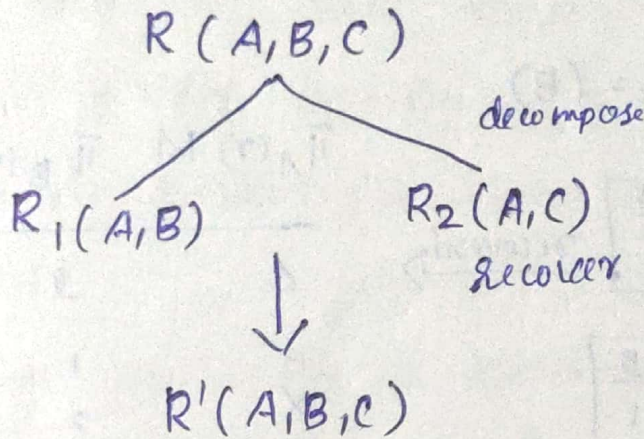


# Decomposition

2

When we decompose a rdb schema with a set of fds  $F$  into  $R_1, \dots, R_n$  we want

1) lossless decomposition :- otherwise decomposition would result in information loss.



$R(A, B, C) = R'(A, B, C) \rightarrow$  lossless decomp:

A decomposition of  $R$  into  $R_1$  &  $R_2$  is lossless form iff atleast one of the following condition is

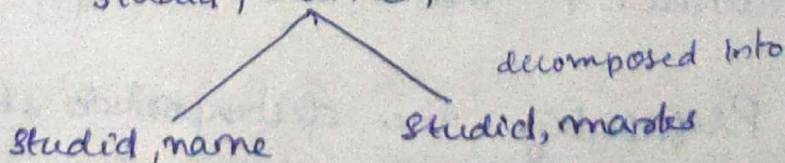
(i)  $F^+$ .

$$R_1 \cap R_2 \rightarrow R_1$$

$$R_2 \cap R_1 \rightarrow R_2$$

## Example

Table having fields  
studid, name, marks.



There is a common attribute studid & original information can be retrieved without any information loss.

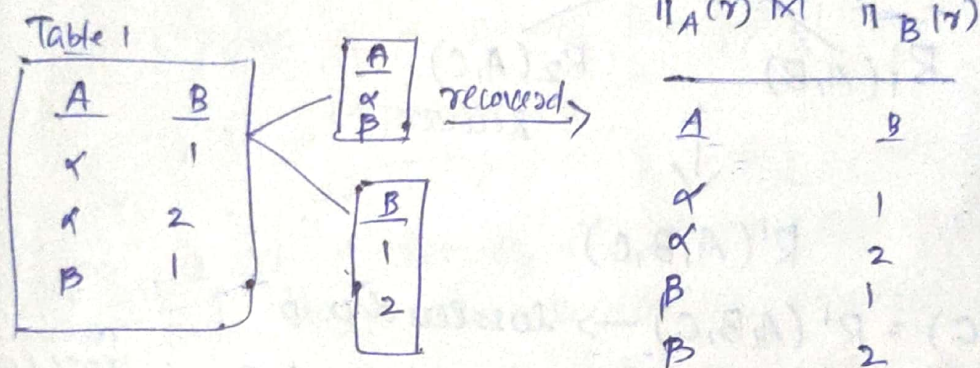


## Illustration of lossy decomposition

Given instances of the decomposed relns, if we are not able to reconstruct the corresponding instances of the original reln - there is information loss i.e. lossy decomposition.

eg:-  $R = (A, B)$

$R_1 = (A), R_2 = (B)$



The original reln is not retrieved after applying decomposition & retrieving data, so this comes under lossy decomposition.

(2) No redundancy :- The reln  $R_i$  shld be either Boyce Codd Normal form or 3rd Normal form.

(3) Dependency preserving :- Let  $F_i$  be the set of dependencies  $F^+$  that include only attributes in  $R_i$ .

Preferably the decomposition shld be dependency preserving, that is

$$(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$$



Otherwise, checking updates for violation in functional dependencies may require computing joins, which is expensive.

Let  $F' = F_1 \cup F_2 \cup \dots \cup F_n$ .  $F'$  is a set of f.d.s on schema  $R$ , but in general  $F' \neq F$ , it may be  $F'^+ = F^+$ . If the latter is true then every dependency in  $F$  is logically implemented in  $F'$ , & if we verify that  $F'$  is satisfied, we have verified that  $F$  is satisfied.

The conclusion is decomposition having the property  $F'^+ = F^+$  is a dependency-preserving decomposition.

### Example

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

## Normalization

The basic objectives of normalization is to reduce redundancy, which means that information is to be stored only once. Storing information several times leads to wastage of storage space &  $\uparrow$  in the total size of the data stored. Relations are normalized so that when alters in the db



are to be altered, we do not lose information or introduce inconsistencies.

## Functional Dependency

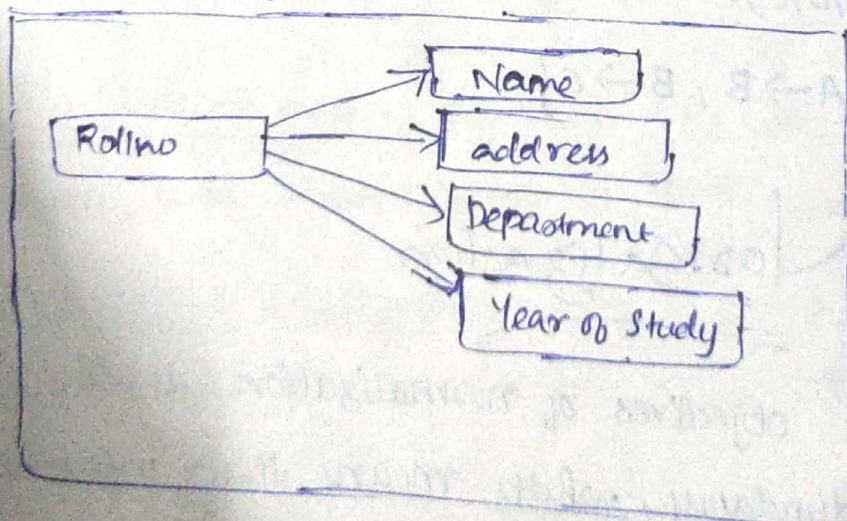
Let  $X$  &  $Y$  be two attributes of a rdb. Given the value of  $X$ , if there is only one value of  $Y$  corresponding to it, then  $Y$  is said to be functionally dependent on  $X$ . This is indicated by the notation.

$$X \rightarrow Y$$

if we write,

$X, Z \rightarrow Y$  — It means that there is only one value of  $Y$  corresponding to given values of  $X, Z$ .

Student



In this rdb named student, the values of all the attributes can be uniquely determined.

Thus all the attributes are f.d on the attribute Rollno.



# Anomalies in a db / Pitfalls in a Reltn Dd

Consider the rlttn

<u>Name</u>	<u>course</u>	<u>Phno</u>	<u>Major</u>	<u>Prof</u>	<u>Grade</u>
Jones	353	237-46843	CS	Smith	A
Smith	329	431-53876	Phy	Turner	B
Martin	456	531-64789	Chem	Clark	B
Duke	293	444-75689	Math	James	A+
Jones	379	237-46843	Histy	Lant.	B

The keys of the rlttns is Name & course.  
Here the attribute grade is fully f'd on the key,  
Name & course.

Name  $\leftarrow$  phone no

Name  $\leftarrow$  Major

Course  $\leftarrow$  Professor

Name, course  $\leftarrow$  Grade

Thus, the determinants of these f'd.  $\neq$  not the entire key, but only part of the key of the rlttn.

The anomalies forced here are.

\* Update Anomalies :- A change in the phno. of Jones must be made, for consistency in all tuples pertaining to the student Jones.



\* Insestion Anomalies :- If this is the only rltm in the db showing the association b/w a faculty member & the course, the fact that a given professor is teaching a given course cannot be entered in the db unless a student is registered in the course.

\* Deletion Anomalies :- If the only student registered in a given course discontinues the course the information as to which professor is offering the course will be lost, if this is the only rltm in the db showing the association b/w a faculty member & the course.

→ It often leads to generation of spurious tuples.

⇒ First Normal Form

- ① The domain of the attributes must include only atomic values
- ② It was designed to disallow multivalued, composite attributes & their combination.
- ③ It disallows nested rltms.

Converting a rltm to 1NF is the 1<sup>st</sup> essential step of normalization. Each form is an improvement over the earlier form - 2NF is an improvement on 1NF, 3NF is an improvement on 2NF & so on.



## Student R1tn

<u>Rollno</u>	<u>Name</u>	<u>Department</u>	<u>Year</u>	<u>Phnno</u>
1	Anju	MCA	1	234567
2	Mary	MBA	2	417892
3	Clare	MCA	1	499435
4	Jist	MBA	2	498763
5	Latha	Btech	3	235865

The above r1tn is in 1NF, as it does not contain any non atomic value, or composite attribute or multivalued attribute.

## Second Normal Form

- ① A r1tn is said to be in 2NF, if it is <sup>already</sup> 1NF & non-key attributes are fully functionally dependent on the 1<sup>o</sup> key attribute.
- ② If the key has more than one attribute then no non-key attributes shld be fd upon part of the key attribute.

### Student R1tn

<u>studid</u>	<u>Name</u>	<u>Courseid</u>	<u>Course name</u>	<u>Grade</u>
101	John	MS1250	Btech	A+
102	John	MS1415	MBA	A
103	Tennon	MS1931	Hot Mgt	B+
104	Chris	MS1455	MCA	B

Primary key — studid, courseid

studid ← Name → partial dependency

Courseid ← Course name → "

studid, courseid ← Grade → full "



create or replace f. seqt. no / no numbers (3)

To convert this into 2NF.

Student

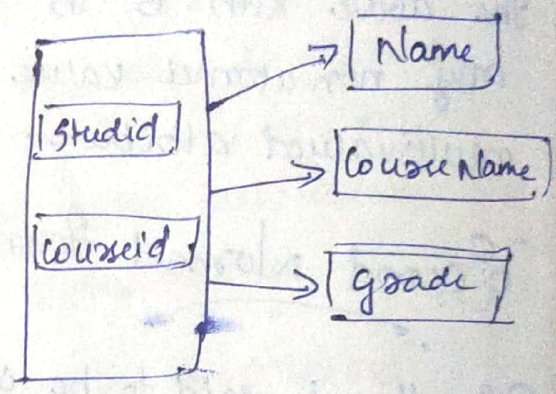
<u>Studid</u>	<u>Name</u>
101	Johns
102	Lennon
103	Chris

Course

<u>Courseid</u>	<u>Coursename</u>
MSI250	Btech
MSI415	MBA
MSI331	Hotl Mng
MSI455	MCA

Student-Grade

<u>Studid</u>	<u>Courseid</u>	<u>Grade</u>
101	MSI250	A+
101	MSI415	A
103	MSI331	B+
103	MSI455	B



Third Normal Form

A table is in 3NF iff

- (1) It is already in 2NF &
- (2) No two non-prime attributes should be f.d on each other i.e. all the non-prime attributes should be non-transitively dependent on each other in the r.tn.

<u>Rollno</u>	<u>Name</u>	<u>Dptmnt</u>	<u>year</u>	<u>hostel</u>
1784	Raman	Phy	1	ganga
1896	Maya	Chem	1	ganga
1487	Singh	Maths	2	Kareem
1693	Rajan	CS	2	"
1847	Krishnan	CS	3	Krishna



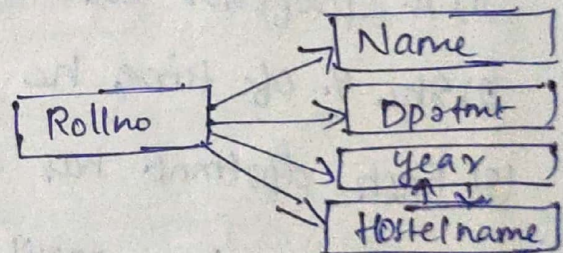
Observe that given the year of student, his hostel is known & vice versa.

Here, dependency is b/w the attributes year & hostel names, which are both non key attributes. It leads to unnecessary duplication of data.

To convert this into 3NF,

<u>Rollno</u>	<u>Name</u>	<u>Dptmnt</u>	<u>year</u>
1784	Raman	Phy	1
1896	Maya	Chem	1
1487	Singh	Maths	2
1693	Rajan	CS	2
1847	Krishnan	CS	3

<u>year</u>	<u>Hostelname</u>
1	Janga
2	Kaivesi
3	Krishna
4	Godavari



### ⊛ Boyce-Codd Normal Form (BCNF)

It arises when

- 1) The table is already in 3NF.
- 2) A attr has more than one possible key.
- 3) Further that the composite keys have a common attribute.
- 4) If any attribute of a composite key is dependent on the attribute of the other composite key, a normalization, BCNF is required.



## Example - Professor

<u>Professor</u>	<u>Department</u>	<u>HOD</u>	<u>Percent</u>
P <sub>1</sub>	Phy	Rao	50
P <sub>1</sub>	Maths	Krishnan	30
P <sub>2</sub>	Chem	Ghosh	75
P <sub>2</sub>	Phy	Rao	95
P <sub>3</sub>	Maths	Krishnan	25

2. The rltm is in 3NF, but the attributes dept & HOD is duplicated.

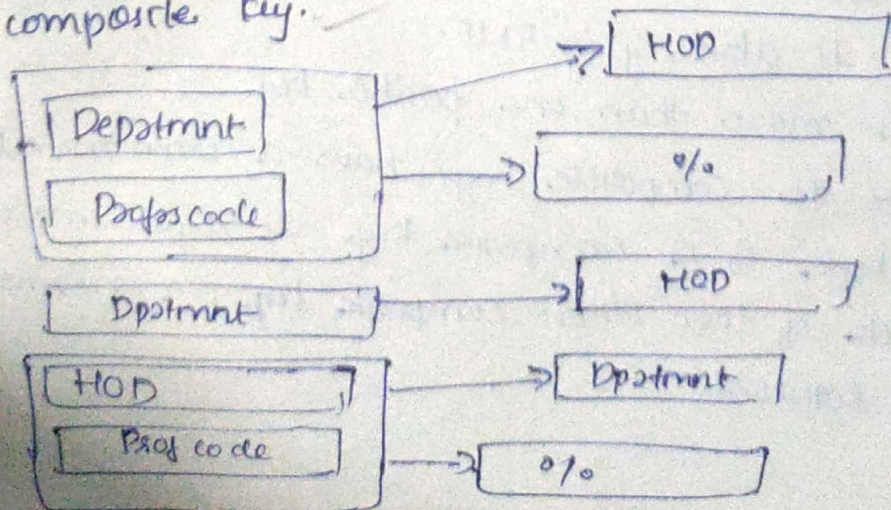
• It is assumed that,

- (1) A professor can work in more than one dept.
- (2) The % of time he spends in each dept is given
- (3) Each department has only one HOD.

The two possible composite keys are HOD,

Professor code & Prof code & Dept ~~other~~

Observe that HOD & department are not non-key attributes, they are part of the composite key.

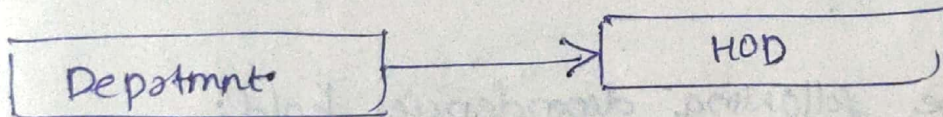
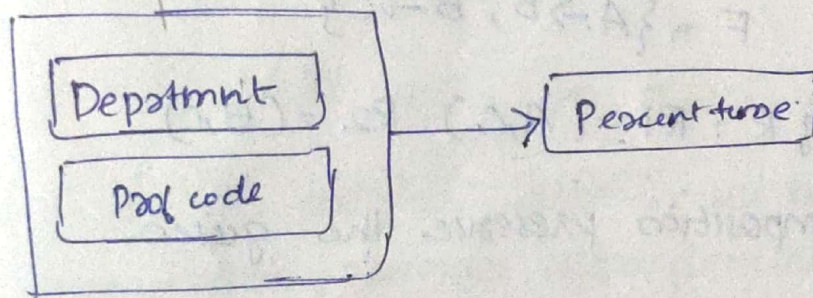




To convert to BCNF,

<u>Profcode</u>	<u>Dpatmnt</u>	<u>% time</u>
P <sub>1</sub>	Phy	50
P <sub>1</sub>	Maths	30
P <sub>2</sub>	Chem	75
P <sub>2</sub>	Phy	75
P <sub>3</sub>	Maths	25

HOD	
Phy	Rao
Maths	Kaushman
Chem	Ghosh



Thus, a table is in BCNF iff it is already in 3NF & every determinant shld be candidate key.

- 1NF → Values shld be non-redundant & atomic
- 2NF → non-prime attributes shld be fully fundamentally dependent.
- 3NF → intertransitively dependent
- 4NF → No multivalued dependency
- 5NF → No join dependency
- 6NF → every determinant shld be a candidate key.



## \* Dependency Preservation

Getting lossless decomposition is necessary. But of course, we also want to keep dependencies, since losing a dependency means, that the corresponding constraint can be checked only through natural join of the appropriate resultant rth in the decomposition. This would be very expensive, so, our aim is to get a lossless dependency preserving decomposition.

Example:

$$R = (A, B, C) \quad F = \{A \rightarrow B, B \rightarrow C\}$$

$$\text{Decomposition of } R: R_1 = (A, C) \quad R_2 = (B, C)$$

? Does this decomposition preserve the given dependencies?

Soln:- In  $R_1$  the following dependencies hold:

$$F_1' = \{A \rightarrow A, C \rightarrow C, A \rightarrow C, AC \rightarrow AC\}$$

$$\text{In } R_2, \quad " \quad " \quad F_2' = \{B \rightarrow B, C \rightarrow C, B \rightarrow C, BC \rightarrow BC\}$$

The set of nontrivial dependencies hold on  $R_1 \& R_2$ :

$$F' := \{B \rightarrow C, A \rightarrow C\}$$

$A \rightarrow B$  can not be derived from  $F'$ , so this decomposition is NOT dependency preserving.



## Example

$$R = (A, B, C)$$

$$F = \{A \rightarrow B, B \rightarrow C\}$$

Decomposition of  $R$ :  $R_1 = (A, B)$

$$R_2 = (B, C)$$

? Does this decomposition preserve the given dep?

Ans

In  $R_1$  the foll: dep holds:

$$F_1 = \{A \rightarrow B, A \rightarrow A, B \rightarrow B, AB \rightarrow AB\}$$

$$F_2 = \{B \rightarrow B, C \rightarrow C, B \rightarrow C, BC \rightarrow BC\}$$

$$F' = F_1 \cup F_2 = \{A \rightarrow B, B \rightarrow C, \text{trivial dependencies}\}$$

In  $F'$  all the original dependencies occur, so this decomposition preserves dependencies.



# Module-IV

## \* Functional Dependencies

Let  $x$  &  $y$  be the two attributes of a relation.  
 Given the value of  $x$ , if there is only one value for  $y$  corresponding to it, then  $y$  is said to be functionally dependent on  $x$ .  
 Indicated by notation  $x \rightarrow y$ .  $y$  is functionally dependent upon  $x$ .

## \* Inference Rules for Functional Dependencies / Armstrong's

Arms' ax. used to conclude  $F_{inferred}$  on a rel. db. w/ a type of assertions (it can apply to a set of FD to derive other FD).  
 axioms & the basis

1. Reflexive Rule: If  $y \subseteq x$ , then  $x \rightarrow y$ .  
 Example:  $x = \{a, b, c, d\}$ ,  $y = \{a, b, c\}$

2. Augmentation Rule: if  $x \rightarrow y$ , then  $xz \rightarrow yz$ .  
 Example:  $R(A, B, C, D)$ , if  $A \rightarrow B$  then  $AC \rightarrow BC$

3. Transitive Rule: if  $x \rightarrow y$  &  $y \rightarrow z$ , then  $x \rightarrow z$ .

4. Decomposition or Projective Rule: if  $x \rightarrow yz$ , then  $x \rightarrow y$  &  $x \rightarrow z$ .

5. Union or Additive Rule: if  $x \rightarrow y$  &  $x \rightarrow z$ , then  $x \rightarrow yz$ .

6. Pseudo Transitive Rule: if  $x \rightarrow y$  &  $wy \rightarrow z$ , then  $wx \rightarrow z$ .

eg.  $R = (A, B, C, G, H, I)$

- $F = \{$
- $A \rightarrow B$
- $A \rightarrow C$
- $CG \rightarrow H$
- $CG \rightarrow I$
- $B \rightarrow H \}$

Sound: that generally and that actually holds something completely general all that hold. They are ax.



# Module-IV

## \* Functional Dependencies

Let  $x$  &  $y$  be the two attributes of a rdn.  
 Given the value of  $x$ , if there is only one value for  $y$  corresponding to it, then  $y$  is said to be functionally dependent on  $x$ .  
 Indicated by notation  $x \rightarrow y$ . *y is funci depend upon x.*

## \* Inference Rules for Functional Dependencies / Armstrong's

• An ax used to conclude  $F_{2nd}$  on a rdn db. W  $F_{1st}$  is assertion it can be derived from a set of FD to derive other FD. *axioms*

1. Reflexive Rule: If  $y \subseteq x$ , then  $x \rightarrow y$   
*Example: name  $\rightarrow$  id, addr.  $x = \{a, b, c, d\}$ ,  $y = \{a, b, c\}$*

2. Augmentation Rule: if  $x \rightarrow y$ , then  $xz \rightarrow yz$   
*Example:  $R(A, B, C, D)$ , if  $A \rightarrow B$  then  $AC \rightarrow BC$*

3. Transitive Rule: if  $x \rightarrow y$  &  $y \rightarrow z$ , then  $x \rightarrow z$

4. Decomposition or Projective Rule: if  $x \rightarrow yz$ , then  $x \rightarrow y$  &  $x \rightarrow z$

5. Union or Additive Rule: if  $x \rightarrow y$  &  $x \rightarrow z$ , then  $x \rightarrow yz$ .

6. Pseudo Transitive Rule: if  $x \rightarrow y$  &  $wy \rightarrow z$ , then  $wx \rightarrow z$

eg.  $R = (A, B, C, G, H, I)$

- $F = \{$
- $A \rightarrow B$
- $A \rightarrow C$
- $CG \rightarrow H$
- $CG \rightarrow I$
- $B \rightarrow H$
- $\}$

Sound: that generated by the rules actually holds in all rdn.  
 Complete: gener all fd that hold. They are...



# find functional dependencies (F+) of F

①  $\rightarrow A \rightarrow B \quad A \rightarrow C$

Union:  $A \rightarrow B, C$

②  $\rightarrow CG \rightarrow H, I \quad CG \rightarrow I$

Union:  $CG \rightarrow H, I$

③  $\rightarrow A \rightarrow B$

$AG \rightarrow CG \rightarrow$  Augment:  $- G$

$CG \rightarrow H$

$\rightarrow AG \rightarrow H$  (transitivity rule)

④  $A \rightarrow B$  (given)

$B \rightarrow H$  (given)

$A \rightarrow H$  (transitivity rule)

$A \rightarrow C = AG \rightarrow CG$  Augment

$CG \rightarrow H$  given

$\rightarrow AG \rightarrow H$  transitivity

• Minimal sets of functional dependencies /  
Minimal canonical cover

A canonical cover of  $F$  (F+) a minimal set of functional dependencies equivalent to  $F$ , having no redundant dependencies / redundant parts of dependencies.

eg:  $\{A \rightarrow B, B \rightarrow C\}$ , He informed from that  $A \rightarrow C$ .



A set of functional dependencies  $F$  to be minimal, it should satisfy the following condition -

- every dependency in  $F$  has a single attribute for its RHS.
- We cannot remove a dependencies from  $F$  & have a set of dependencies that is equivalent to  $F$ .
- We can't replace any dependency  $\alpha \rightarrow A$  in  $F$  with a dependency  $\gamma \rightarrow A$  where  $\gamma \subset \alpha$  & still have a set of dependencies that is equivalent to  $F$ .

$\alpha = \{A \rightarrow B, B \rightarrow C, A \rightarrow CD\}$  *Redundant*

$\gamma = \{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$  *minimal*

OR

$\alpha = \{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$  *Remove, exp. transitivity*

$\gamma = \{A \rightarrow B, B \rightarrow C\}$  *minimal*

$\gamma \subset \alpha$

\* Normalization

Reduce redundancies & inconsistencies (data correct)

? First Normal Form:

The domains of the attribute must include only atomic values. It was design to disallow multivalued, composite attributes & their combination. (nested str)



eg:- Student

Rollno	Name	Dept	Year	phonenumber
1	Anju	MCA	1	234567
2	Merry	MBA	2	467892
3	clairi	MCA	1	489435
4	rust	MBA	2	498763
5	-	Btech	3	-

### ♥ Second Normal Form

A rltb is said to be (fn) 2NF, if it is already in 1NF & the non-key attributes are fully functionally dependent upon the primary key attribute.

eg:- Student Relation

Studid	Name	courseid	course name	Grade
101	Johnson	MSI250	Mtech	A+
101	Johnson	MSI415	MBA	A
102	kennin	MSI331	Hotelman	B+
103	chois	MSI455	MCA	B

Primary key - studid, courseid

studid  $\leftarrow$  Name

courseid  $\leftarrow$  course name

studid, courseid  $\leftarrow$  grade

(depend on 2 primary key)



Solution

stud

studid	Name
101	Johnson
102	Lennis
103	Chris

COURSE

courseid	coursename	grade
MS1250	Mtech	A+
MS1415	MBA	A
MS1331	Hotel Mng	B+
MS1455	MCA	B

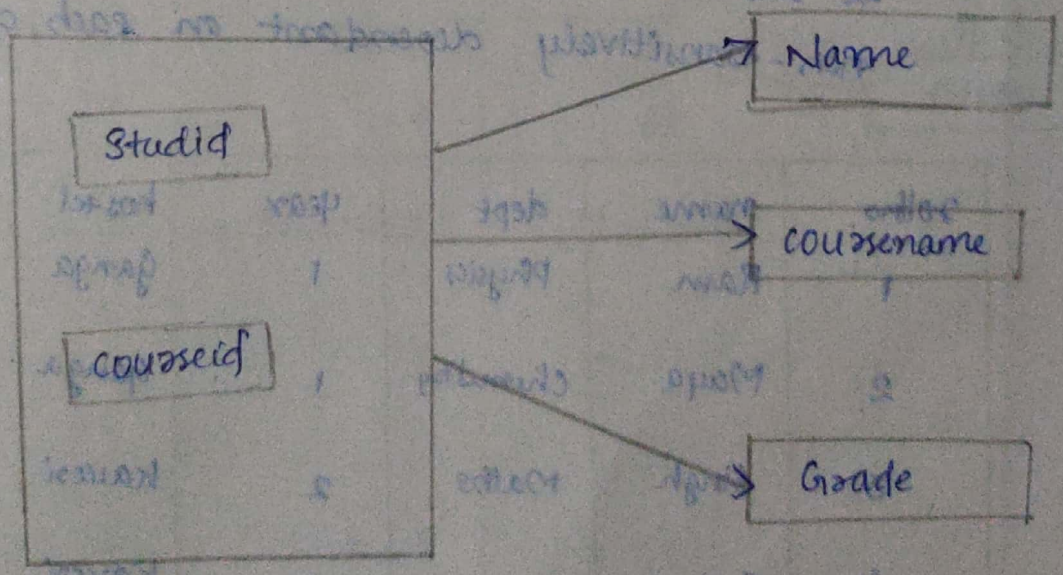
studid → name

courseid ← coursename → grade

studid	courseid	grade
101	MS1250	A+
101	MS1415	A
102	MS1331	B+
103	MS1455	B

StudGrade

studid, courseid → grade





book

foreign key bookid references tablenam

bookid	bookname
101	...
201	...
301	...

bookid number (3)

book name varchar(4)

foreign key bookid references author

### • Third Normal Form

A table is in 3NF, iff:

(i) It is already in 2NF

(ii) No two non-prime attributes should be functionally dependent on each other.  
ie all the non-prime attributes should be non-transitively dependant on each other.

rollno	name	dept	year	hostel
1	Ram	Physics	1	Ganga
2	Maya	Chemistry	1	Ganga
3	Singh	Maths	2	Kaveri
4	Rajan	CS	2	Kaveri
5	Krishnan	CS	8	Krishna

given by  
study of  
has/his  
can be  
with  
depending  
course  
hostel, which  
not non-prime  
non-key attribute  
primary dependant  
on data

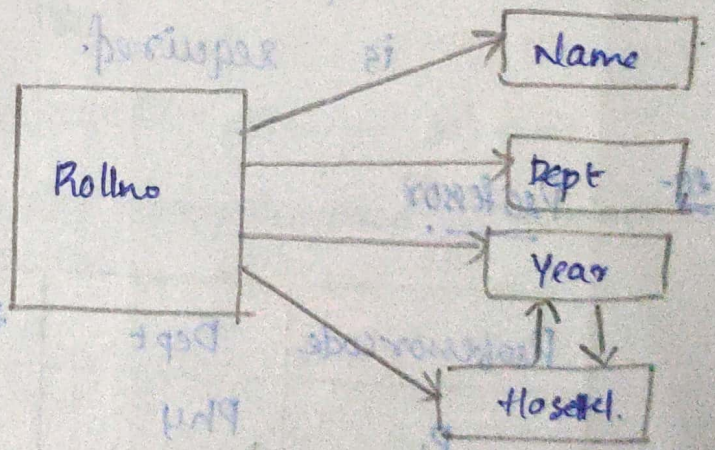


(i) student Normal form (1NF)

rollno	name	dept	year
1	Ram	Phy	Ganga 1
2	Maya	Chem	Ganga 1
3	Singh	Maths	Kaveri 2
4	Rajan	CS	Kaveri 2
5	Krishnan	CS	Kaveri 3

(ii) stud-hosel composite key

Year	hosel
1	Ganga
2	Kaveri
3	Krishna.





# Boyce-Codd Normal Form (BCNF)

BCNF arises when:

- (a) the table is already in 3NF.
- (b) A rltn has more than one possible key.  
 eg. Profcode & Dept OR Profcode & HOD
- (c) furthermore, the composite keys have a common attribute  
 eg. more than 1 attr as key → Profcode
- (d) If an attribute of a composite key is dependent on the attribute of the other composite key, a normalization BCNF is required.  
 eg. dependent Dept & HOD

Professor

Professorcode	Dept	Head of Dept	Percent
P <sub>1</sub>	Phy	Rao	50
P <sub>1</sub>	Maths	Krishnam	30
P <sub>2</sub>	Chem	Ghosh	60
P <sub>3</sub>	Phy	Rae	25
P <sub>3</sub>	Maths	Krishman	30

one dept has only 1 HOD  
 each dept keys - composite key  
 people & dept OR Profcode & HOD  
 Maths - Phy the same dept  
 redundancy  
 dependency - HOD of Dept  
 non-prime - not part of composite key



Profcode	Dept	Percent	Dept	Associate HOD
P <sub>1</sub>	Phy	50	Phy	Rao
P <sub>1</sub>	Maths	30	Maths	Krishnan
P <sub>2</sub>	Chem	60	chem	Ghosh.
P <sub>2</sub>	Phy	25		
P <sub>3</sub>	Maths	30		

### Fourth Normal Form

A rdn is in 4NF iff :

- (i) It is already in BCNF
- (ii) It contains non-trivial multivalued dependencies.

⇒ multivalued attribute

multivalued dependencies (MVD)

$A \twoheadrightarrow B$  MVD represents a dependencies between attributes

$A \twoheadrightarrow C$  eg: A, B & C is a rdn S, for each value of A, there is a set of value for B & a set of values for C.

B & C are independent

However the set of values of B & C are independent of each other.



eg:- ModelNo

Manufacturing  
Year

colour

M101

2010

Red

M101

2010

Black

M102

2013

Red

M102

2014

Black

M103

2014

Red

model / manufacturing year  
model / color

ModelNo → Manufacturing yr

ModelNo → colour

Manufacturing yr & colour are independent to each other.

eg of 4NF

Vendor - supply - Projects reln.

tab: VendorSupply

Vendorcode	Itemcode	Projectcode
V <sub>1</sub>	I <sub>1</sub>	P <sub>1</sub>
V <sub>1</sub>	I <sub>2</sub>	P <sub>1</sub>
V <sub>2</sub>	I <sub>2</sub>	P <sub>2</sub>
V <sub>2</sub>	I <sub>3</sub>	P <sub>2</sub>
V <sub>3</sub>	I <sub>1</sub>	P <sub>3</sub>

Vendorcode	Itemcode
V <sub>1</sub>	I <sub>1</sub>
V <sub>1</sub>	I <sub>2</sub>
V <sub>2</sub>	I <sub>2</sub>
V <sub>2</sub>	I <sub>3</sub>
V <sub>3</sub>	I <sub>1</sub>



table-2

VendorProject

Vendorcode	ProjectNo
V <sub>1</sub>	P <sub>1</sub>
V <sub>2</sub>	P <sub>2</sub>
V <sub>3</sub>	P <sub>3</sub>

$A \twoheadrightarrow B$

Studname, address  $\twoheadrightarrow$  address

A MVD can be classified as trivial & non-trivial.

An MVD  $A \twoheadrightarrow B$  in a reltn is defined as being trivial,

if B is a subset of A.

### \* Fifth Normal Form

A reltn is said to be 5NF, iff

1. It is already in 4NF

2. There should not be any join dependencies

eg:- table vendor supply

table 1

Vendorcode	Itemcode
V <sub>1</sub>	I <sub>1</sub>
V <sub>1</sub>	I <sub>2</sub>
V <sub>2</sub>	I <sub>2</sub>
V <sub>2</sub>	I <sub>3</sub>
V <sub>3</sub>	I <sub>1</sub>

Projects reltn

table: 2

Vendorcode	Projectcode
V <sub>1</sub>	P <sub>1</sub>
V <sub>2</sub>	P <sub>2</sub>
V <sub>3</sub>	P <sub>3</sub>



Tables.

Itemcode	Projectcode
I <sub>1</sub>	P <sub>1</sub>
I <sub>2</sub>	P <sub>1</sub>
I <sub>2</sub>	P <sub>2</sub>
I <sub>3</sub>	P <sub>2</sub>
I <sub>1</sub>	P <sub>3</sub>

- Pitfalls in a relational database / Anomalies in db.

Stud. grade

Name	Course	Phnno	Major	Professor	Grade
Jones	353	23746843	CS	Smith	A
Smith	329	43153876	Physics	Turner	B
Martin	456	531-64789	Chemistry	Dart	B
Pike	293	444-78689	Maths	James	A+
Jones	379	237-4683	History	Lamb	A

- Update Anomalies
- Insertion Anomalies
- Deletion Anomalies



- Name  $\leftarrow$  Phn no
- Name  $\leftarrow$  Major
- Course  $\leftarrow$  Professor
- Name course  $\leftarrow$  grade

The anomalies freed here are

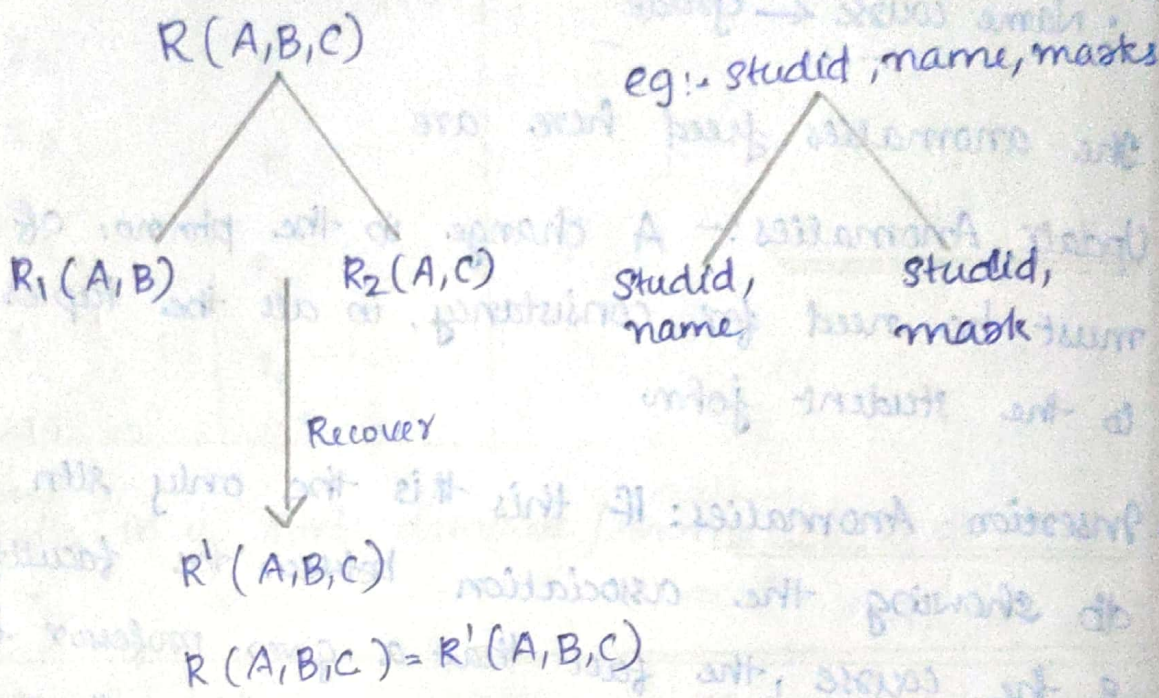
- Update Anomalies: - A change in the phn no: of johns must be need for consistency, in all the tuples pertaining to the student john
- Insertion Anomalies: If this is the only sltn in the db showing the association between the faculty member & the course, the fact that a given professor is teaching a given course cannot be entered in the db unless a student is registered in the course.
- Deletion Anomalies: If the only student registered in the given course discontinues the course the info that has to which professor is offering the course will be lost, if this is the only sltn in the db showing the Association b/w a faculty member & the course.

Lead to inconsistency



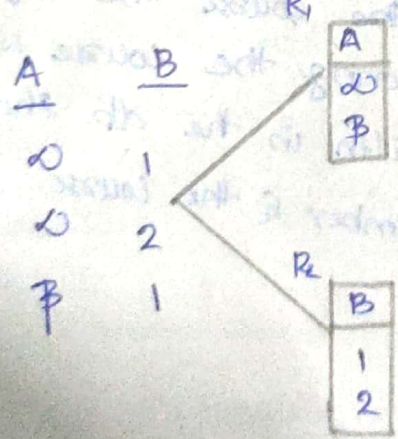
→ Properties of Relational Decomposition :- lossless & lossy

• Lossless join Decomposition :-



• Lossy Decomposition :-

$R = (A, B)$



A	B
$\alpha$	1
$\alpha$	2
$\beta$	1
$\beta$	2



## • Property 1

After decomposing & trying to retrieve original data, if the original information is lost it comes under lossy decomposition.

If we are able to retrieve or reconstruct the original data that we had before applying decomposition even after decomposing & joining the table it comes under lossless decomposition.

The point here is that when we apply decomposition, it should be lossless decomposition.

## • Property 2

+ No Redundancy

The relation should be either in BCNF or in 3NF.

We want to keep dependencies since losing a dependency means the corresponding constraint can be checked only through natural join of the appropriate resultant relation in the decomposition.

This could be very expensive, so our aim is to get a lossless dependency preserving decomposition.

Example:  $R = (A, B, C)$ ,  $F = (A \rightarrow B, B \rightarrow C)$

Decomposition of  $R$ :  $R_1 = (A, C)$ ,  $R_2 = (B, C)$

Solution: In  $R_1$  the following dependencies hold:  $F' = (A \rightarrow A, C \rightarrow C, A \rightarrow C, AC \rightarrow AC)$

augm  $\rightarrow AC \rightarrow AC$   
reflex  $\rightarrow AC \rightarrow AC$



In  $R_2$  the following dependencies hold:  $F^2 = (B \rightarrow B, c \rightarrow c, B \rightarrow c, BC \rightarrow BC)$

The set of dependencies hold on  $R_1 \cup R_2$ :  $\{B \rightarrow c\}, A \rightarrow B$  cannot be derived so decomposition is not dependency preserving.

Example-1

$R = (A, B, C) \quad F = (A \rightarrow B, B \rightarrow C)$

Decomposition of  $R$ :  $R_1 = (A, B), R_2 = (B, C)$

Does the decomposition preserve the given dependencies?

ans:- In  $R_1$  the following dependencies hold:  $F^1 = (A \rightarrow A, B \rightarrow B, B \rightarrow A, AB \rightarrow AB)$

In  $R_2$  the following dependencies hold:  $F^2 = (B \rightarrow B, C \rightarrow C, C \rightarrow B, BC \rightarrow BC)$

The set of dependencies hold on  $R_1 \cup R_2 = \{A \rightarrow B, B \rightarrow C\}$

This decomposition preserves the functional dependencies given in the original, & etc.